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Roll No.

Total Questions: 13]

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B.C.A. IInd Semester Examination, May-2019

MATHEMATICS-II

(BCA 201)

(New)

Time: 3 Hrs. |

[M.M. : 75

Note:— Attempt all the Sections as per instructions.

Section-A

(Very Short Answer Type Questions)

- **Note** :- Attempt all the *five* questions. Each question carries 3 marks.
- Differentiate finite sets and infinite sets with example.
- Define trigonometric function, exponential function and logarithmic function.

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Turn Over

- 3. What do you mean by 'Principle of Duality' ?
- 4. If $u = f\left(\frac{y}{x}\right)$ then prove that :

$$x\frac{\partial u}{\partial x} + y\frac{\partial u}{\partial y} = 0$$

5. Evaluate the triple integral $\int_0^1 \int_1^2 \int_2^3 dx \, dy \, dz$.

Section-B

(Short Answer Type Questions)

Note: Attempt any two questions out of the following three questions. Each question carries 5 marks.

- Define equivalence relation. If A = {1, 2, 3, 4} and R = {(1, 1), (1, 2), (2, 1), (2, 2), (3, 4), (4, 3) (3, 3), (4, 4)}. Then prove that R is an equivalent relation.
- 7. Find the area of the region bounded by the circle $x^2 + y^2 = a^2$, by double integration.
- 8. Show that the lines $\frac{x-1}{2} = \frac{y-2}{3} = \frac{z-3}{4}$ and 4x 3y + 1 = 0 = 5x 3z + 2 are coplanar. Also find their point of intersection.

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Section-C

(Long Answer Type Questions)

- **Note**:— Attempt any *three* questions out of the following five questions. Each question carries 15 marks.
- 9. (i) If Q be the set of rational numbers and f: Q → Q be defined by f(x) = 2x + 3 then prove that f is bijective. Also find f⁻¹.
 - (ii) If $f: \mathbb{R} \to \mathbb{R}$ and $g: \mathbb{R} \to \mathbb{R}$ be defined by f(x) = x 1 and $g(x) = x^2 + 1$ then find $f \circ g(1)$, $f \circ g(2)$, $g \circ g(2)$.
- 10. (i) Let (L, ≤) is a lattice. If a, b ∈ L then prove that:

$$a \le b \Leftrightarrow a \land b = a$$

and $a \le b \Leftrightarrow a \lor b = b$

(ii) Let (L, \leq) be a lattice with least element 0 and greatest element 1. If $a \in L$ then show that:

$$a \vee 1 = 1$$
 and $a \wedge 1 = a$

Also $a \lor 0 = a$ and $a \land 0 = 0$

) (i) Discuss the maxima or minima of the function:

$$u = xy + \left(\frac{a^3}{x}\right) + \left(\frac{a^3}{y}\right)$$

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(ii) If
$$u = \log \left(\frac{x^2 + y^2}{x + y} \right)$$
 then prove that:

$$x\frac{\partial u}{\partial x} + y\frac{\partial u}{\partial y} = 1$$

- 12. (i) Show that the lines $\frac{x+1}{-3} = \frac{y-3}{2} = \frac{z+2}{1}$ and $\frac{x}{1} = \frac{y-7}{-3} = \frac{z+7}{2}$ are coplanar.
 - (ii) Find the angle of intersection of the spheres: $x^2 + y^2 + z^2 - 2x - 4y - 6z + 10 = 0$ and $x^2 + y^2 + z^2 - 6x - 2y + 2z + 2 = 0$
- 13. (i) Evaluate the double integral $\int_0^a \int_0^{\sqrt{(a^2-x^2)}} x^2 y \, dx \, dy$. Also mention the region of integration involved in this double integral.
 - (ii) Prove that the value of triple integration:

$$\int_0^1 \int_0^{\sqrt{(1-x^2)}} \int_0^{\sqrt{(1-x^2-y^2)}} xyz \, dz \, dy \, dx, \text{ is } \frac{1}{48}.$$

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